

Question 1.

Solution:

(i) 441
 $= 3 \times 3 \times 7 \times 7$

$$\begin{array}{r|l} 3 & 441 \\ \hline 3 & 147 \\ \hline 7 & 49 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (7)^2 = (21)^2$$

\therefore 441 is a perfect square

(ii) $576 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3$
 $\times 3$

$$\begin{array}{r|l}
 2 & 576 \\
 \hline
 2 & 288 \\
 \hline
 2 & 144 \\
 \hline
 2 & 72 \\
 \hline
 2 & 36 \\
 \hline
 2 & 18 \\
 \hline
 3 & 9 \\
 \hline
 3 & 3 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= (2)^2 \times (2)^2 \times (2)^2 \times (3)^2 \\
 &= (2 \times 2 \times 2 \times 3)^2 = (24)^2
 \end{aligned}$$

\therefore 576 is a perfect square

(iii) $11025 = 3 \times 3 \times 5 \times 5 \times 7 \times 7$

$$\begin{array}{r|l}
 3 & 11025 \\
 \hline
 3 & 3675 \\
 \hline
 5 & 1225 \\
 \hline
 5 & 245 \\
 \hline
 7 & 49 \\
 \hline
 7 & 7 \\
 \hline
 & 1
 \end{array}$$

$$\begin{aligned}
 &= (3)^2 \times (5)^2 \times (7)^2 \\
 &= (3 \times 5 \times 7)^2 = (105)^2
 \end{aligned}$$

\therefore 11025 is a perfect square

(iv) $1176 = 2 \times 2 \times 2 \times 3 \times 7 \times 7$

$$\begin{array}{r|l}
 2 & 1176 \\
 \hline
 2 & 588 \\
 \hline
 2 & 294 \\
 \hline
 3 & 147 \\
 \hline
 7 & 49 \\
 \hline
 7 & 7 \\
 \hline
 & 1
 \end{array}$$

$$= (2)^2 \times 2 \times 3 \times (7)^2$$

1176 is not a perfect square as it cannot be expressed as the product of pair of equal factors

(v) $5625 = 3 \times 3 \times 5 \times 5 \times 5 \times 5$

$$\begin{array}{r|l}
 3 & 5625 \\
 \hline
 3 & 1875 \\
 \hline
 5 & 625 \\
 \hline
 5 & 125 \\
 \hline
 5 & 25 \\
 \hline
 5 & 5 \\
 \hline
 & 1
 \end{array}$$

$$= (3)^2 \times (5)^2 \times (5)^2$$

$$= (3 \times 5 \times 5)^2 = (75)^2$$

\therefore 5625 is a perfect square

(vi) $9075 = 3 \times 5 \times 5 \times 11 \times 11$

$$\begin{array}{r|l}
 3 & 9075 \\
 \hline
 5 & 3025 \\
 \hline
 5 & 605 \\
 \hline
 11 & 121 \\
 \hline
 11 & 11 \\
 \hline
 & 1
 \end{array}$$

$$= 3 \times (5)^2 \times (11)^2$$

\therefore 9075 is not a perfect square as it cannot be expressed as a product of pair of equal factors

(vii) $4225 = 5 \times 5 \times 13 \times 13$

$$\begin{array}{r|l} 5 & 4225 \\ \hline 5 & 845 \\ \hline 13 & 169 \\ \hline 13 & 13 \\ \hline & 1 \end{array}$$

$$= (5)^2 \times (13)^2$$

$$= (5 \times 13)^2 = (65)^2$$

$\therefore 4225$ is a perfect square

(viii) $1089 = 3 \times 3 \times 11 \times 11$

$$\begin{array}{r|l} 3 & 1089 \\ \hline 3 & 363 \\ \hline 11 & 121 \\ \hline 11 & 11 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (11)^2$$

$$= (3 \times 11)^2 = (33)^2$$

$\therefore 1089$ is a perfect square

Question 2.**Solution:**

(i) $1225 = 5 \times 5 \times 7 \times 7$

$$\begin{array}{r|l}
 5 & 1225 \\
 \hline
 5 & 245 \\
 \hline
 7 & 49 \\
 \hline
 7 & 7 \\
 \hline
 & 1
 \end{array}$$

$$= (5)^2 \times (7)^2 = (5 \times 7)^2$$

$$= (35)^2$$

Hence it is a perfect square and it is the square of 35

(ii) $2601 = 3 \times 3 \times 17 \times 17$

$$\begin{array}{r|l}
 3 & 2601 \\
 \hline
 3 & 867 \\
 \hline
 17 & 289 \\
 \hline
 17 & 17 \\
 \hline
 & 1
 \end{array}$$

$$= (3)^2 \times (17)^2 = (3 \times 17)^2 = (51)^2$$

Hence it is a perfect square and it is the square of 51

(iii) $5929 = 7 \times 7 \times 11 \times 11$

$$\begin{array}{r|l}
 7 & 5929 \\
 \hline
 7 & 847 \\
 \hline
 11 & 121 \\
 \hline
 11 & 11 \\
 \hline
 & 1
 \end{array}$$

$$= (7)^2 \times (11)^2 = (7 \times 11)^2 = (77)^2$$

It is a perfect square and is the the square of 77

$$(iv) 7056 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7 \times 7$$

$$\begin{array}{r|l} 2 & 7056 \\ \hline 2 & 3528 \\ \hline 2 & 1764 \\ \hline 2 & 882 \\ \hline 3 & 441 \\ \hline 3 & 147 \\ \hline 7 & 49 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$= (2)^2 \times (2)^2 \times (3)^2 \times (7)^2$$

$$= (2 \times 2 \times 3 \times 7)^2 = (84)^2$$

\therefore It is a perfect square and is of the square of 84

$$(v) 8281 = 7 \times 7 \times 13 \times 13$$

$$\begin{array}{r|l} 7 & 8281 \\ \hline 7 & 1183 \\ \hline 13 & 169 \\ \hline 13 & 13 \\ \hline & 1 \end{array}$$

$$= (7)^2 \times (13)^2$$

$$= (7 \times 13)^2 = (91)^2$$

\therefore It is a perfect square and is of the square of 91

Question 3.

Solution:

(i) Factors of 3675

$$3 \times 5 \times 5 \times 7 \times 7$$



$$\begin{array}{r|l}
 3 & 3675 \\
 5 & 1225 \\
 5 & 245 \\
 7 & 49 \\
 7 & 7 \\
 & 1
 \end{array}$$

$$= 3 \times (5)^2 \times (7)^2$$

∴ In order to get a perfect square the given number should be multiplied by 3

(ii) $2156 = 2 \times 2 \times 7 \times 7 \times 11$

$$\begin{array}{r|l}
 2 & 2156 \\
 2 & 1078 \\
 7 & 539 \\
 7 & 77 \\
 11 & 11 \\
 & 1
 \end{array}$$

$$= (2)^2 \times (7)^2 \times 11$$

In order to get a perfect square, the given number should be multiplied by 11

(iii) $3332 = 2 \times 2 \times 7 \times 7 \times 17$

$$\begin{array}{r|l}
 2 & 3332 \\
 2 & 1666 \\
 7 & 833 \\
 7 & 119 \\
 17 & 17 \\
 & 1
 \end{array}$$

$$= (2)^2 \times (7)^2 \times 17$$

In order to get a perfect square, the given number should be multiplied by 17

$$(iv) 2925 = 3 \times 3 \times 5 \times 5 \times 13$$

$$\begin{array}{r|l} 3 & 2925 \\ \hline 3 & 975 \\ \hline 5 & 325 \\ \hline 5 & 65 \\ \hline 13 & 13 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (5)^2 \times 13$$

In order to get a perfect square, the given number must be multiplied by 13

$$(v) 9075 = 3 \times 5 \times 5 \times 11 \times 11$$

$$\begin{array}{r|l} 3 & 9075 \\ \hline 5 & 3025 \\ \hline 5 & 605 \\ \hline 11 & 121 \\ \hline 11 & 11 \\ \hline & 1 \end{array}$$

$$= 3 \times (5)^2 \times (11)^2$$

In order to get a perfect square, the given number must be multiplied by 3

$$(vi) 7623 = 3 \times 3 \times 7 \times 11 \times 11$$

$$\begin{array}{r|l} 3 & 7623 \\ \hline 3 & 2541 \\ \hline 7 & 847 \\ \hline 11 & 121 \\ \hline 11 & 11 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (11)^2 \times 7$$

In order to get a perfect square, the given number should be multiplied by 7

$$(vii) 3380 = 2 \times 2 \times 5 \times 13 \times 13$$

$$\begin{array}{r|l} 2 & 3380 \\ \hline 2 & 1690 \\ \hline 5 & 845 \\ \hline 13 & 169 \\ \hline 13 & 13 \\ \hline & 1 \end{array}$$

$$= (2)^2 \times 5 \times (13)^2$$

In order to get a perfect square, the given number must be multiplied by 5

$$(viii) 2475 = 3 \times 3 \times 5 \times 5 \times 11$$

$$\begin{array}{r|l} 3 & 2475 \\ \hline 3 & 825 \\ \hline 5 & 275 \\ \hline 5 & 55 \\ \hline 11 & 11 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (5)^2 \times 11$$

In order to get a perfect square the given number must be multiplied by 11

Question 4.

Solution:

(i) 1575

$$= 3 \times 3 \times 5 \times 5 \times 7$$

$$\begin{array}{r|l} 3 & 1575 \\ \hline 3 & 525 \\ \hline 5 & 175 \\ \hline 5 & 35 \\ \hline 7 & 7 \\ \hline & 1 \end{array}$$

$$= (3)^2 \times (5)^2 \times 7$$

In order to get a perfect square, the given number must be divided by 7

(ii) $9075 = 3 \times 5 \times 5 \times 11 \times 11$

$$\begin{array}{r|l}
 3 & 9075 \\
 5 & 3025 \\
 5 & 605 \\
 11 & 121 \\
 11 & 11 \\
 \hline
 & 1
 \end{array}
 = 3 \times (5)^2 \times (11)^2$$

In order to get a perfect square, the given number must be divided by 3

(iii) $4851 = 3 \times 3 \times 7 \times 7 \times 11$

$$\begin{array}{r|l}
 3 & 4851 \\
 3 & 1617 \\
 7 & 539 \\
 7 & 77 \\
 11 & 11 \\
 \hline
 & 1
 \end{array}
 = (3)^2 \times (7)^2 \times 11$$

In order to get a perfect square, the given number be divided by 11

(iv) $3380 = 2 \times 2 \times 5 \times 13 \times 13$

$$\begin{array}{r|l}
 2 & 3380 \\
 2 & 1690 \\
 5 & 845 \\
 13 & 169 \\
 13 & 13 \\
 \hline
 & 1
 \end{array}$$

$$= (2)^2 \times 5 \times (13)^2$$

In order to get a perfect square, the given number must be divided by 5

(v) $4500 = 2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 5$

$$\begin{array}{r|l} 2 & 4500 \\ 2 & 2250 \\ 3 & 1125 \\ 3 & 375 \\ 5 & 125 \\ 5 & 25 \\ 5 & 5 \\ & 1 \end{array}$$

$$= (2)^2 \times (3)^2 \times (5)^2 \times 5$$

In order to get a perfect square, the given number must be divided by 5

(vi) $7776 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3$

$$\begin{array}{r|l} 2 & 7776 \\ 2 & 3888 \\ 2 & 1944 \\ 2 & 972 \\ 2 & 486 \\ 3 & 243 \\ 3 & 81 \\ 3 & 27 \\ 3 & 9 \\ 3 & 3 \\ & 1 \end{array}$$

$$= (2)^2 \times (2)^2 \times 2 \times 3 \times (3)^2 \times (3)^2$$

In order to get a perfect square, the given number must be divided by 2×3 i.e., 6

$$(vii) 8820 = 2 \times 2 \times 3 \times 3 \times 5 \times 7 \times 7$$

$$\begin{array}{r|l} 2 & 8820 \\ 2 & 4410 \\ 3 & 2205 \\ 3 & 735 \\ 5 & 245 \\ 7 & 49 \\ 7 & 7 \\ & 1 \end{array}$$

$$= (2)^2 \times (3)^2 \times 5 \times (7)^2$$

In order to get a perfect square, the given number must be divided by 5

$$(viii) 4056 = 2 \times 2 \times 2 \times 3 \times 13 \times 13$$

$$\begin{array}{r|l} 2 & 4056 \\ 2 & 2028 \\ 2 & 1014 \\ 3 & 507 \\ 13 & 169 \\ 13 & 13 \\ & 1 \end{array}$$

$$= (2)^2 \times 2 \times 3 \times (13)^2$$

In order to get a perfect square, the given number must be divided by 2×3 i.e., 6

Question 5.

Solution:

The largest two digit number = 99

$$\begin{array}{r} 9 \\ 9 \overline{) 99} \\ \underline{81} \\ 18 \end{array}$$

Finding the square root of 99, we get remainder = 18

∴ The greatest two digit number which is a perfect square will be = $99 - 18 = 81$

Question 6.

Solution:

The largest 3 digit number = 999

$$\begin{array}{r} 31 \\ 3 \overline{) 999} \\ \underline{9} \\ 61 \\ 61 \overline{) 99} \\ \underline{61} \\ 38 \end{array}$$

Finding the square root of 999, we get remainder = 38

∴ The greatest 3 digit number which is a perfect square = $999 - 38 = 961$